## SCALE EFFECTS IN THE POST-CRACKING BEHAVIOUR OF CNT-EPOXY COMPOSITES: PREDICTING CRACK JUMPS AND DUCTILE-TO-BRITTLE TRANSITIONS

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## Abstract

The scale effects on the global structural response of fibre-reinforced brittle-matrix specimens subjected to bending are discussed in the framework of Fracture Mechanics by means of the Updated Bridged Crack Model (UBCM). This analytical model assumes the composite as a bi-phase material, in which both the brittle matrix and the reinforcing fibres contribute to the global toughness [1-3]. In particular, the bridging mechanism of the reinforcing layers can be described by an appropriate cohesive softening constitutive law, which takes into account the progressive slippage of the fibre inside the matrix [4,5]. In addition, the discontinuous phenomena, i.e., crack jumps (snap-back) and snap-through instabilities, which experimentally characterize the post-cracking behaviour of the composite, can be captured in a quantitative way [1]. Furthermore, UBCM predicts different post-cracking regimes depending on two dimensionless numbers: the *reinforcement brittleness number*,  $N_{\rm P}$ , which is related to the fibre volume fraction,  $V_{\rm f}$ , and the pull-out brittleness number,  $N_w$ , which is related to the fibre embedment length,  $w_c$ .  $N_P$  turns out to govern the stability of the fracturing process, whereas  $N_w$  is able to describe the softening tail of the nonsmooth post-cracking evolution [4]. Both these dimensionless numbers depend on the beam depth, h, which, keeping the other variables to be constant, drives a ductile-to-brittle transition in the post-cracking regime of the composite. The critical value of the reinforcement brittleness number,  $N_{PC}$ , allows to predict the minimum (critical) specimen size,  $h_{\min}$ , which, analogously to the minimum fibre volume fraction,  $V_{f,\min}$ , is required to achieve a stable post-cracking response. Finally, UBCM simulations of non-smooth crack evolutions are compared to experimental results reported in the scientific literature [6], in which carbon nanotube-epoxy specimens are tested in bending (Figs. 1,2).



Figure 1. Failure of CNT-epoxy in bending (a); Pull-out nanotube bundles bridging the crack before failure (b) [6].



Figure 2. UBCM modelling of the non-smooth post-cracking evolution of a CNT-epoxy specimen in bending.

## References

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